Capacity Allocation in Multi-cell UMTS Networks for Different Spreading Factors with Perfect and Imperfect Power Control

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Abstract

An analytical model for calculating capacity in multi-cell UMTS networks is presented. Capacity is maximized for different spreading factors and for perfect and imperfect power control. An analytical model is presented for approximating the user distributions in multi-cell third generation WCDMA networks using 2-dimensional Gaussian distributions by determining the means and the standard deviations of the distributions for every cell. This allows for the calculation of the inter-cell interference and the reverse-link capacity of the network. The capacity was determined for signal-to-interference threshold from 5 dB to 10 dB and spreading factor values of 256, 64, 16, and 4.

1. Introduction

3G cellular systems are identified as International Mobile Telecommunications-2000 under International Telecommunication Union and as Universal Mobile Telecommunications Systems (UMTS) by European Telecommunications Standards Institute. Besides voice capability in 2G, the new 3G systems are required to have additional support on a variety of data-rate services using multiple access techniques. Code Division Multiple Access (CDMA) is the fastest-growing digital wireless technology since its first commercialization in 1994. The major markets for CDMA are North America, Latin America, and Asia (particularly Japan and Korea). In total, CDMA has been adopted by more than 100 operators across 76 countries around the globe [1].

Since the first comparisons of multiple access schemes for UMTS [2], which found that Wideband CDMA (WCDMA) was well suited for supporting variable bit rate services, several research on

WCDMA capacity has been considered. In [3], the authors present a method to calculate the WCDMA reverse link Erlang capacity based on the Lost Call Held (LCH) model as described in [4]. This algorithm calculates the occupancy distribution and capacity of UMTS/WCDMA systems based on a system outage condition. The authors derive a closed form expression of Erlang capacity for a single type of traffic loading and compare analytical results with simulations results.

The same LCH model was also used in [5] to calculate the forward link capacity of UMTS/WCDMA systems based on the system outage condition. In the forward link, because many users share the base station (BS) transmission power, the capacity is calculated at the BS. The transmission power from the BS is provided to each user based on each user's relative need. The access in the calculation of forward link capacity is one-to-many rather than many-to-one as in the reverse link. The authors provide capacity calculation results and performance evaluation through simulation.

An alternate approach, where mobile stations (MSs) are synchronized on the uplink, i.e., signals transmitted from different MSs are time aligned at the BS, has been considered. Synchronous WCDMA looks at time synchronization for signal transmission between the BS and MS to improve network capacity. The performance of an uplink-synchronous WCDMA is analyzed in [6]. Scrambling codes are unique for each cell. MSs in the same cell share the same scrambling code, while different orthogonal channelization codes are derived from the set of Walsh codes. In [6], the potential capacity gain is about 35.8% in a multi-cell scenario with infinite number of channelization codes per cell and no soft handoff capability between MSs and BSs. However, the capacity gain in a more realistic scenario is reduced to 9.6% where soft handoff is enabled. The goal of this uplink-synchronous method in WCDMA is

to reduce intra-cell interference. But the implementation is fairly complex while the potential capacity gain is not very high.

In this work, we will calculate the maximum reverse link capacity in UMTS/WCDMA systems for both perfect and imperfect power control with a given set of quality of service requirements and for different spreading factors.

The remainder of this paper is organized as follows. The user and interference models are presented in Section 2. In Sections 3 and 4, we analyze capacity for perfect and imperfect power control, respectively. Spreading factors are discussed in Section 5. Numerical results are presented in Section 6, and finally Section 7 concludes the paper.

2. User and Interference Model

This study assumes that each user is always communicating and is power controlled by the BS that has the highest received power at the user. Let $r_i(x, y)$ and $r_j(x, y)$ be the distance from a user to BS i and BS j , respectively. This user is power controlled by BS j in the cell or region C_j with area A_j , which BS j services. This study assumes that both large scale path loss and shadow fading are compensated by the perfect power control mechanism. Let $I_{ji,g}$ be the average inter-cell interference that all users $n_{j,g}$ using services g with activity factor v_g and received signal S_g at BS j impose on BS i . Modifying the average inter-cell interference given by [7], it becomes

$$I_{ji}^{(g)} = S_g v_g n_{j,g} \frac{e^{(\beta\sigma_s)^2}}{A_j} \int \int_{C_j} \frac{r_j^m(x, y)}{r_i^m(x, y)} w(x, y) dA(x, y), \quad (1)$$

where $\beta = \ln(10)/10$, σ_s is the standard deviation of the attenuation for the shadow fading, m is the path loss exponent, and $w(x, y)$ is the user distribution density at (x, y) . Let $\kappa_{ji,g}$ be the per-user (with service g) relative inter-cell interference factor from cell j to BS i ,

$$\kappa_{ji,g} = \frac{e^{(\beta\sigma_s)^2}}{A_j} \int \int_{C_j} \frac{r_j^m(x, y)}{r_i^m(x, y)} w(x, y) dA(x, y). \quad (2)$$

The inter-cell interference density I_{ji}^{inter} from cell j to BS i from all services G becomes

$$I_{ji}^{inter} = \frac{1}{W} \sum_{g=1}^G I_{ji}^{(g)}, \quad (3)$$

where W is the bandwidth of the system. Eq. (3) can be rewritten as

$$I_{ji}^{inter} = \frac{1}{W} \sum_{g=1}^G S_g v_g n_{j,g} \kappa_{ji,g}. \quad (4)$$

Thus, the total inter-cell interference density I_i^{inter} from all other cells to BS i is

$$I_i^{inter} = \frac{1}{W} \sum_{j=1, j \neq i}^M \sum_{g=1}^G S_g v_g n_{j,g} \kappa_{ji,g}, \quad (5)$$

where M is the total number of cells in the network.

If the user distribution density can be approximated, then, $\kappa_{ji,g}$ needs to be calculated only once. The user distribution is modeled with a 2-dimensional Gaussian function as follows [8]

$$w(x, y) = \frac{\eta}{2\pi\sigma_1\sigma_2} e^{-\frac{1}{2}(\frac{x-\mu_1}{\sigma_1})^2} e^{-\frac{1}{2}(\frac{y-\mu_2}{\sigma_2})^2}, \quad (6)$$

where η is a user density normalizing parameter.

By specifying the means μ_1 and μ_2 and the standard deviations σ_1 and σ_2 of the distribution for every cell, an approximation can be found for a wide range of user distributions ranging from uniform to hot-spot clusters. These results are compared with simulations to determine the value of η experimentally.

3. WCDMA Capacity with Perfect Power Control

In WCDMA, with perfect power control (PPC) between BSs and MSs, the energy per bit to total interference density at BS i for a service g is given by [9]

$$\left(\frac{E_b}{I_0}\right)_{i,g} = \frac{\frac{S_g}{R_g}}{N_0 + I_i^{inter} + I_i^{own} - S_g v_g}, \quad (7)$$

where N_0 is the thermal noise density, and R_g is the bit rate for service g . I_i^{inter} was calculated in section 2. I_i^{own} is the total intra-cell interference density caused by all users in cell i . Thus I_i^{own} is given by

$$I_i^{own} = \frac{1}{W} \sum_{g=1}^G S_g v_g n_{i,g}. \quad (8)$$

Let τ_g be the minimum signal-to-noise ratio, which must be received at a BS to decode the signal of a user with service g , and S_g^* be the maximum signal power, which the user can transmit. Substituting (5) and (8) into (7), we have for every cell i in the WCDMA network, the number of users $n_{i,g}$ in BS i for a given service

g needs to meet the following inequality constraints

$$\tau_g \leq \frac{\frac{S_g^*}{R_g}}{N_0 + \frac{S_g^*}{W}} \left[\sum_{g=1}^G n_{i,g} v_g + \sum_{j=1, j \neq i}^M \sum_{g=1}^G n_{j,g} v_g \kappa_{ji,g} - v_g \right], \quad (9)$$

for $i=1, \dots, M$.

After rearranging terms, (9) can be rewritten as

$$\sum_{g=1}^G n_{i,g} v_g + \sum_{j=1, j \neq i}^M \sum_{g=1}^G n_{j,g} v_g \kappa_{ji,g} - v_g \leq c_{eff}^{(g)}, \quad (10)$$

for $i=1, \dots, M$,

where

$$c_{eff}^{(g)} = \frac{W}{R_g} \left[\frac{1}{\tau_g} - \frac{R_g}{S_g^*/N_0} \right]. \quad (11)$$

The maximized capacity in a WCDMA network is defined as the maximum number of simultaneous users $(n_{1,g}, n_{2,g}, \dots, n_{M,g})$ for all services $g = 1, \dots, G$ that satisfy (10).

4. WCDMA Capacity with Imperfect Power Control

The calculation of WCDMA network capacity, which was formulated in section 3, assumes perfect power control between the BSs and MSs. However, transmitted signals between BSs and MSs are subject to multi-path propagation conditions, which make the received $\left(\frac{E_b}{I_o}\right)_{i,g}$ signals vary according to a log-normal distribution with a standard deviation on the order of 1.5 to 2.5 dB [4]. Thus, in the imperfect power control (IPC) case, the constant value of $(E_b)_{i,g}$ in each cell i for every user with service g needs to be replaced by the variable $(E_b)_{i,g} \triangleq \epsilon_{i,g}(E_b)_{o,g}$, which is log-normally distributed. We define

$$x_{i,g} = 10 \log_{10} \left(\frac{\epsilon_{i,g}(E_b)_{o,g}}{I_0} \right), \quad (12)$$

to be a normally distributed random variable with mean m_c and standard deviation σ_c .

According to [4], by evaluating the n th moment of $\epsilon_{i,g}$ using the fact that $x_{i,g}$ is Gaussian with mean m_c and standard deviation σ_c , then taking the expected value, we have

$$E \left[\frac{(E_b)_{o,g}}{I_0} \epsilon_{i,g} \right] = \frac{(E_b)_{i,g}}{I_0} e^{\frac{(\beta \sigma_c)^2}{2}}. \quad (13)$$

As a result of (13), $c_{eff-IPC}^{(g)}$ becomes $c_{eff}^{(g)} / e^{\frac{(\beta \sigma_c)^2}{2}}$.

Figure 1. Generation of OVFS codes for different Spreading Factors.

5. Spreading Factor

Communication from a single source is separated by channelization codes, i.e. the dedicated physical channel in the uplink and the downlink connections within one sector from one MS. The Orthogonal Variable Spreading Factor (OVFS) codes, which were originally introduced in [10], were used to be channelization codes for UMTS.

The use of OVFS codes allows the orthogonality and spreading factor (SF) to be changed between different spreading codes of different lengths. Fig. 1 depicts the generation of different OVFS codes for different SF values.

6. Numerical Results

The results shown are for a twenty-seven cell network topology used in [11, 12]. The COST-231 propagation model with a carrier frequency of 1800 MHz, average base station height of 30 meters and average mobile height of 1.5 meters, is used to determine the coverage region. The path loss coefficient m is 4. The shadow fading standard deviation σ_s is 6 dB. The processing gain $\frac{W}{R_g}$ is 6.02 dB, 12.04 dB, 18.06 dB, and 24.08 dB for Spreading Factor equal to 4, 16, 64, and 256, respectively. The activity factor, v , is 0.375. Fig. 2 shows the 2-D Gaussian approximation of users uniformly distributed in the cells with $\sigma_1 = \sigma_2 = 12000$.

The WCDMA network with 27 omnidirectional antenna cells (1 sector per cell) was analyzed for evaluation of capacity using user modeling with the 2-D Gaussian function and traditional methods of model-

Figure 2. 2-D Gaussian approximation of users uniformly distributed in the cells. $\sigma_1 = \sigma_2 = 12000$, $\mu_1 = \mu_2 = 0$.

ing uniform user distribution. The network with different values for $\frac{E_b}{I_0}$ was analyzed for different SF values of 4, 16, 64, and 256.

6.1. Capacity Allocation with SF of 256

First, we set SF to 256, which is used to carry data for the control channel. Fig. 3 shows the maximized average number of slots per sector for the 27 cells WCDMA network as the $\frac{E_b}{I_0}$ is increased from 5 dB to 10 dB and the standard deviation of imperfect power control is increased from 0 to 2.5 dB. Because of IPC, to get the same average number of slots per sector as PPC, we have to decrease the SIR threshold by 0.5 dB to 1.5 dB. Fig. 3 also shows that the traditional uniform user distribution modeling matches well with the 2-D Gaussian model.

6.2. Capacity Allocation with SF of 64

As a result of lowering the SF to 64, the number of slots per sector decreases by almost a factor of 4 compared to SF equal 256 (from 60.58 to 15.56 slots when $\frac{E_b}{I_0} = 7.5$ dB in PPC) as shown in Fig. 4.

6.3. Capacity Allocation with SF of 16

As a result of lowering the SF to 16, the number of slots per sector decreases by almost a factor of 4 compared to SF equal 64 (from 15.56 to 4.30 slots when $\frac{E_b}{I_0} = 7.5$ dB in PPC) as shown in Fig. 5.

6.4. Capacity Allocation with SF of 4

Next, we set SF to 4, which is used for 256 kbps data communication between BSs and MSs. As a result of

Figure 3. Average number of slot per sector for perfect and imperfect power control analysis with a Spreading Factor of 256.

Figure 4. Average number of slot per sector for perfect and imperfect power control analysis with a Spreading Factor of 64.

Figure 5. Average number of slot per sector for perfect and imperfect power control analysis with a Spreading Factor of 16.

Figure 6. Average number of slot per sector for perfect and imperfect power control analysis with a Spreading Factor of 4.

lowering the SF to 4, the number of slots per sector decreases significantly to 1.49 while keeping $\frac{E_b}{I_o} = 7.5$ dB in PPC as shown in Fig. 6.

7. Conclusions

An analytical model has been presented for calculating capacity in multi-cell WCDMA networks. Numerical results show that the SIR threshold for the received signals is decreased by 0.5 to 1.5 dB due to the imperfect power control. As expected, we can have many low rate voice users or fewer data users as the data rate increases. The results also show that the determined parameters of the 2-dimensional Gaussian model matches well with traditional methods for modeling uniform user distribution. Our method of maximizing capacity is fast, accurate, and can be implemented for large multi-cell UMTS networks.

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